

Algebra

MONDAY 2-25-13

CLASS NOTES

(EX) $x^{\frac{1}{2}} = \sqrt{x}$ or (\sqrt{x})

FER #7 $a^{\frac{N}{M}} = \sqrt[M]{a^N}$ or $(\sqrt[M]{a})^N$

MR $a^M \cdot a^N = a^{M+N}$

DR $\frac{a^M}{a^N} = a^{M-N}$

ZER $\frac{a^M}{a^M} = 1 = a^0$
EX. $0^0 = 0$

NER $a^{-N} = \frac{1}{a^N}$ or

$\frac{1}{a^{-N}} = a^N$

PPR $(a^M)^N = a^{M \cdot N}$

GPR $\left(\frac{ab}{cd}\right)^N = \frac{a^N b^N}{c^N d^N}$

NER

$$\frac{a^4}{a^7} = \frac{\cancel{aaaa}}{\cancel{aaaa}aa} = \frac{1}{a^3}$$

$$a^{4-7} = a^{-3} = \frac{1}{a^3}$$

$$\frac{1}{a^{-3}} = \frac{1}{\frac{1}{a^3}} = 1 \cdot \frac{a^3}{1} = a^3$$

$$\begin{aligned}
 (49) \quad \frac{(-2N) \cdot 2N}{(-N)^{-1}} &= \frac{2N(-N)^1}{(-N)^{-1}} \\
 &= 2N \cdot -N \\
 &= \boxed{-2N^2}
 \end{aligned}$$

$$\begin{aligned}
 (51) \quad -\frac{X^3 \cdot X^2}{(-X^{-3})^{-4}} &= -\frac{X^5}{(-X)^{12}} \\
 &= +\frac{X^5}{X^{12}} = -X^{-7} \\
 &= \boxed{-\frac{1}{X^7}}
 \end{aligned}$$

(90)

$$\begin{aligned}
 & \frac{K^{\frac{1}{2}}}{\left(K^{\frac{1}{3}}\right)^{\frac{1}{5}} \left(K^{\frac{1}{2}}\right)^{\frac{1}{10}}} \\
 & \frac{K^{\frac{3}{2}}}{K^{\frac{5}{9}} K^{\frac{1}{3}}} = \frac{K^{\frac{3}{2}}}{K^{\frac{5}{9}} K^{\frac{3}{9}}} \\
 & = \frac{K^{\frac{3}{2}}}{K^{\frac{8}{9}}} \\
 & = K^{\frac{3}{2} - \frac{8}{9}} \\
 & = K^{\frac{27}{18} - \frac{16}{18}} \\
 & = K \\
 & = \boxed{K^{\frac{11}{18}}} \quad \checkmark
 \end{aligned}$$

(92)

$$\frac{(X^3)^{\frac{1}{3}}}{X^{\frac{1}{3}} \cdot X}$$

$$= \frac{X^{\frac{1}{3}}}{X^{\frac{1}{3}} \cdot X^{\frac{1}{3}}}$$

$$= \frac{X^2}{X^{\frac{2}{3}}}$$

$$= \frac{X^{\frac{12}{6}}}{X^{\frac{16}{6}}}$$

$$= X^{\frac{12-16}{6}} = X^{-\frac{4}{6}} = X^{-\frac{2}{3}}$$

$$= \frac{1}{X^{\frac{2}{3}}} \cdot \frac{X^{\frac{1}{3}}}{X^{\frac{1}{3}}} = \boxed{\frac{X^{\frac{1}{3}}}{X}}$$