

Algebra

Monday 4-15-13

Class Notes

Ch. 8-6 Solving Quadratic Equations By Factoring

IF THEY ARE FACTORABLE

Steps: ① Put in Standard Form

$$ax^2 + bx + c = 0$$

② Factor GCF if there is one

$$\underline{\text{GCF}}(ax^2 + bx + c) = 0$$

③ Factor the quadratic trinomial using magic number method

$$\text{GCF}(ax^2 + bx + c) = 0$$

$$\begin{aligned} \text{sum} &= b \\ \text{prod} &= ac \end{aligned}$$

$$\begin{matrix} \downarrow & \downarrow \\ \square & \square \end{matrix}$$

$$\text{GCF}(\text{binomial})(\text{binomial}) = 0$$

④ Find solutions using ZPP \*

⑤ Check solutions

\* ZPP = zero product property

$$ab = 0$$

$$a = 0 \text{ or } b = 0$$

$$\textcircled{\text{Ex}} \quad 4x^2 = -10x + 6$$

$$4x^2 + 10x - 6 = 0$$

$$\stackrel{2}{=} (2x^2 + 5x - 3) = 0$$

$$\text{sum} = b = 5$$

$$\text{prod} = ac = -6$$

$$\textcircled{-1x + 6x}$$

$$(2x^2 - 1x) + (6x - 3)$$

$$x(2x - 1) + 3(2x - 1)$$

$$\stackrel{2}{=} [(2x - 1)(x + 3)] = 0$$

ZPP

ZPP

$$x = \left\{ \frac{1}{2}, -3 \right\}$$

$$\begin{array}{l} \text{CK} \\ x = \frac{1}{2} \end{array} \quad 4\left(\frac{1}{2}\right)^2 \stackrel{?}{=} -10\left(\frac{1}{2}\right) + 6$$

$$4\left(\frac{1}{2}\right)^2 \stackrel{?}{=} -10\left(\frac{1}{2}\right) + 6$$

$$4\left(\frac{1}{4}\right) \stackrel{?}{=} -5 + 6$$

$$1 \stackrel{?}{=} 1 \checkmark$$

$$\begin{array}{l} \text{CK} \\ x = 3 \end{array} \quad 4(-3)^2 \stackrel{?}{=} -10(-3) + 6$$

$$4(-3)^2 \stackrel{?}{=} -10(-3) + 6$$

$$4(9) \stackrel{?}{=} 30 + 6$$

$$36 = 36 \checkmark$$

①  $16 + 24a = -5a^2$

$5a^2 + 24a + 16 = 0$

Sum = 24  
 prod = 80  
 +4 +20

$(5a^2 + 4a) + (20a + 16) = 0$

$a(5a + 4) + 4(5a + 4) = 0$

$(5a + 4)(a + 4) = 0$

$a = \left\{ -\frac{4}{5}, -4 \right\}$

SF  
 GCF = ?  
 MAGIC NUMBER

FACTORS  
 ZPP

OK  
 $a = -\frac{4}{5}$

$16 + 24\left(-\frac{4}{5}\right) \stackrel{?}{=} -5\left(-\frac{4}{5}\right)^2$

$16 - \frac{96}{5} \stackrel{?}{=} -5\left(\frac{16}{25}\right)$

$\frac{80}{5} - \frac{96}{5} \stackrel{?}{=} -\frac{16}{5} \quad \checkmark$

OKS.

OK  
 $a = -4$

$16 + 24(-4) \stackrel{?}{=} -5(-4)^2$

$16 - 96 \stackrel{?}{=} -5(16)$

$-80 \stackrel{?}{=} -80 \quad \checkmark$

$$\textcircled{7} \quad 0 = -2x^2 - 6 + 7x$$

$$2x^2 - 7x + 6 = 0$$

$$\text{sum} = b = -7$$

$$\text{prod} = ac = 12$$

$$-3 \quad -4$$

$$(2x^2 - 3x) + (-4x + 6) = 0$$

$$x(2x - 3) + -2(2x - 3) = 0$$

$$(2x - 3)(x - 2) = 0$$

$$x = \left\{ \frac{3}{2}, 2 \right\}$$

$$\underline{\underline{OK}}$$
  

$$x = \frac{3}{2}$$

$$0 \stackrel{?}{=} -2\left(\frac{3}{2}\right)^2 - 6 + 7\left(\frac{3}{2}\right)$$

$$0 \stackrel{?}{=} -2\left(\frac{9}{4}\right) - 6 + \frac{21}{2}$$

$$0 \stackrel{?}{=} -\frac{9}{2} - \frac{12}{2} + \frac{21}{2} \quad \checkmark$$

$$\underline{\underline{OK}}$$
  

$$x = 2$$

$$0 \stackrel{?}{=} -2(2)^2 - 6 + 7(2)$$

$$0 \stackrel{?}{=} -8 - 6 + 14 \quad \checkmark$$