3-8 Study Guide and Intervention

Solving Equations and Formulas

Solve for Variables Sometimes you may want to solve an equation such as $V = \ell wh$ for one of its variables. For example, if you know the values of V, w, and h, then the equation $\ell = \frac{V}{wh}$ is more useful for finding the value of ℓ . If an equation that contains more than one variable is to be solved for a specific variable, use the properties of equality to isolate the specified variable on one side of the equation.

Example 1 Solve 2x - 4y = 8 for y.

$$2x - 4y = 8$$

$$2x - 4y - 2x = 8 - 2x$$

$$-4y = 8 - 2x$$

$$\frac{-4y}{-4} = \frac{8 - 2x}{-4}$$

$$y = \frac{8 - 2x}{-4} \text{ or } \frac{2x - 8}{4}$$

The value of *y* is $\frac{2x-8}{4}$.

Example 2

Solve 3m - n = km - 8 for m.

$$3m - n = km - 8$$

$$3m - n - km = km - 8 - km$$

$$3m - n - km = -8$$

$$3m - n - km + n = -8 + n$$

$$3m - km = -8 + n$$

$$m(3 - k) = -8 + n$$

$$\frac{m(3 - k)}{3 - k} = \frac{-8 + n}{3 - k}$$

$$m = \frac{-8 + n}{3 - k}, \text{ or } \frac{n - 8}{3 - k}$$

The value of m is $\frac{n-8}{3-k}$. Since division by 0 is undefined, $3-k \neq 0$, or $k \neq 3$.

Exercises

Solve each equation or formula for the variable specified.

$$1. ax - b = c \text{ for } x$$

2.
$$15x + 1 = y$$
 for x

3.
$$(x + f) + 2 = j$$
 for x

4.
$$xy + z = 9$$
 for y

5.
$$x(4-k) = p$$
 for k

6.
$$7x + 3y = m \text{ for } y$$

7.
$$4(c + 3) = t$$
 for c

$$8. \ 2x + b = c \text{ for } x$$

9.
$$x(1 + y) = z$$
 for x

10.
$$16z + 4x = y$$
 for x

11.
$$d = rt$$
 for r

12.
$$A = \frac{h(a+b)}{2}$$
 for h

13.
$$C = \frac{5}{9}(F - 32)$$
 for F

14.
$$P = 2\ell + 2w \text{ for } w$$

15.
$$A = \ell w$$
 for ℓ