

BE - Alg. I WEDNESDAY 11-12-08

① On the SAME graph (large, at least  $\frac{1}{2}$  page), graph the following two lines:

A.  $y = -2x + 5$

B.  $y = 4x - 1$

② Is  $(2, 1)$  on either line?

③ Is  $(-1, -5)$  on either line?

④ Is  $(0, 0)$  on either line?

⑤ Is  $(1, 3)$  on either line?

②  $(2, 1)$  is an  $(x, y)$  pair on  $y = -2x + 5$   
↓  
pick  $x = 2$ ,  $y = -2(2) + 5 = 1$

③  $(-1, -5)$  is on  $4x - 1$

④  $(0, 0)$  is on neither line.

⑤  $(1, 3)$  is on BOTH Lines!

Every  $(x, y)$  pair on a line is  
 A solution to its linear equation  
 since substituting the  $(x, y)$  pair  
 into the linear equation (in ANY  
 form such as  $y = mx + b$  or  $Ax + By = C$   
 or others) makes a true expression.

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Two lines on the same graph, or  
 two lines "taken together" form a  
"SYSTEM OF LINEAR EQUATIONS."

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Normal Algebra  $\Rightarrow$  use braces

(Ex)

$$\begin{cases} y = -2x + 5 \\ y = 4x - 1 \end{cases}$$


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\*d) The  $(x, y)$  pair where the two lines  
 cross is the solution to the system  
 of linear equations.

2.

You can solve a system of linear equations by graphing... why is this not a good way to do so?

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- \* NOT ACCURATE
  - SLOW
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How can you solve  $\begin{cases} y = 2x + 5 \\ y = 4x - 1 \end{cases}$

using Algebra?

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Two ways, both use (they must) both equations, and both start out by ELIMINATING ONE of the variables.

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- Elimination By Substitution (EBS)
- Elimination By Addition (EBA)

## Elimination By Substitution

- Solve ONE of the equations for  $x$  or  $y$  (4 choices) and then SUBSTITUTE into the other.

(Ex)

$$\left\{ \begin{array}{l} y = -2x + 5 \\ y = 4x - 1 \end{array} \right.$$

*← Already solved for  $y$ , how convenient!*

$$-2x + 5 = 4x - 1$$

$$+2x \qquad +2x$$

LOOK, the  $y$  has been eliminated, you can solve this !!!

$$\begin{array}{r} 5 = 6x - 1 \\ +1 \qquad \qquad +1 \end{array}$$

$$\frac{6}{6} = \frac{6x}{6}$$

$$\boxed{1 = x}$$

$$y = 4(1) - 1 = \boxed{3 = y}$$

Use EITHER Eq. TO FIND  $y$ , they both must work  $\boxed{(1, 3)}$

## Elimination By Addition

- Get the  $x$ ,  $y$ , and numbers lined up (if they are not already) then multiply ONE equation to get equal AND opposite  $x$  terms or  $y$  terms (usually only 2 choices, usually one is better)

(Ex)

$$y = -2x + 5 \xrightarrow{\text{②}} 2y = -4x + 10$$

$$y = 4x - 1 \xrightarrow{\text{+}} \underline{\quad}$$

WHEN YOU ADD →  
THESE, THE  $x$   
IS ELIMINATED!  
YOU CAN SOLVE  
THIS!!

$$\frac{3y}{3} = \frac{9}{3}$$

$$\boxed{y = 3}$$

USE EITHER  
EQUATION  
TO FIND  $x$

$$\begin{array}{rcl} 3 & = & 4x - 1 \\ +1 & & +1 \end{array}$$

$$\boxed{(1, 3)} \checkmark$$

$$\frac{4}{4} = \frac{4x}{4} \therefore \boxed{x = 1}$$

Both EBS and EBA will work  
for ANY system of linear equations,  
usually one way will be EASIER.

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Tip: if a variable is already  
"by itself" use EBS,  
if the X, Y, and numbers are  
already lined up (in the same  
order), use EBA.

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Many options exist:

$$y = -2x + 5 \xrightarrow{\text{(-1)}} -y = 2x - 5$$

$$y = 4x - 1 \rightarrow \underline{y = 4x - 1}$$


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$$\begin{array}{r} 0 = 6x - 6 \\ + 6 \qquad \qquad + 6 \end{array}$$

$$\frac{6}{6} = \frac{6x}{6}$$

$$\boxed{1 = x} \therefore \boxed{y = 3}$$

6.

Determine best method to solve, then  
solve using both methods.

$$2x - y = 6 \xrightarrow{\times 4} 8x - 4y = 24$$

$$3x + 4y = -2 \longrightarrow 3x + 4y = -2$$

$$11x = 22$$

$$x = 2$$

$$\therefore 2(2) - y = 6$$

$$\begin{array}{r} 4 - y = 6 \\ -6 + y \quad -6 + y \\ \hline -2 \quad = \quad y \end{array}$$

$$(2, -2)$$

$$2x - y = 6 \rightarrow y = 2x - 6$$

$$3x + 4(2x - 6) = -2$$

$$3x + 8x - 24 = -2$$

$$11x = 22$$

$$x = 2$$

$$\therefore y = -2$$

Look over Ch. 7-1 to 7-4

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Homework: Pg. 390 # 5 and 6

Solve using BOTH EBS and EBA

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- Check out online Treasure Hunt
- Return graded work
- Midterms this week
- Quiz Fri.  $\Rightarrow$  EBA/EBS