

Precalc - BE | WEDNESDAY 2-10-10

① $(\sqrt{2})^3 = ?$

② $\left(\frac{1}{2}\right)^4 = ?$

③ $0! = ?$

④ $(8x^3)^0 = ?$

① $2\sqrt{2}$

② $\frac{1}{16}$

③ 1

④ 1

Group Practice: Pg. 804 # 23, 25, 29

Precalc -

Homework Review: Pg. 804 # 9, 10, 22

9. ^{*} (6th) term of $(a-b)^7$ $\therefore N=7, r=5$ ^{*}

$$(X+Y)^N = \sum_{r=0}^N \frac{N!}{r!(N-r)!} X^{N-r} Y^r$$

$\downarrow \quad \downarrow$
 $(a) \quad (-b)$

$$= \frac{7!}{5!(2!)} (a)^2 (-b)^5$$

$\uparrow$ ODD power
 STAYS NEGATIVE

$$= \frac{7 \cdot 6}{2} a^2 - b^5 = \boxed{-21a^2 b^5}$$

10. ^{*} (4th) term of $(X+\sqrt{3})^9$ $\therefore N=9, r=3$ ^{*}

$$(X+Y)^N = \sum_{r=0}^N \frac{N!}{r!(N-r)!} X^{N-r} Y^r$$

$\downarrow \quad \downarrow$
 $(X) \quad (\sqrt{3})$

$$= \frac{9!}{3!6!} X^6 (\sqrt{3})^3$$

$$\sqrt{3}\sqrt{3}\sqrt{3} = 3\sqrt{3}$$

$$= \frac{9 \cdot 8 \cdot 7}{3 \cdot 2} \cdot X^6 \cdot 3\sqrt{3}$$

$$\begin{array}{r} 84 \\ \times 3 \\ \hline 252 \end{array}$$

$$= 12 \cdot 7 \cdot 3 X^6 \sqrt{3} = \boxed{252 X^6 \sqrt{3}}$$

$$\textcircled{22} \left(\frac{1}{2}N + 2 \right)^5 \left\{ (X+Y)^N = \sum_{r=0}^N \frac{N!}{r!(N-r)!} x^{N-r} y^r \right.$$

$\downarrow \quad \downarrow$
 $(\frac{1}{2}N) \quad (2)$

$$\Rightarrow \sum_{r=0}^5 \frac{5!}{r!(5-r)!} \left(\frac{1}{2}N \right)^{5-r} (2)^r$$

$$= \frac{5!}{0!5!} \left(\frac{1}{2}N \right)^5 (2)^0 + \frac{5!}{1!(4!)} \left(\frac{1}{2}N \right)^4 (2)^1$$

$$\underbrace{\hspace{10em}}_{r=0}$$

$$\underbrace{\hspace{10em}}_{r=1}$$

$$= \frac{5!}{2!3!} \left(\frac{1}{2}N \right)^3 (2)^2 + \frac{5!}{3!2!} \left(\frac{1}{2}N \right)^2 (2)^3$$

$$\underbrace{\hspace{10em}}_{r=2}$$

$$\underbrace{\hspace{10em}}_{r=3}$$

$$= \frac{5!}{4!(1!)} \left(\frac{1}{2}N \right)^1 (2)^4 + \frac{5!}{5!(0!)} \left(\frac{1}{2}N \right)^0 (2)^5$$

$$\underbrace{\hspace{10em}}_{r=4}$$

$$\underbrace{\hspace{10em}}_{r=5}$$

$$\frac{1}{32}N^5 + \frac{5}{16}N^4(2) + \frac{10}{8}N^3(4) + \frac{10}{4}N^2(8) \dots$$

$$+ \frac{5}{2}N(16) + 32$$

$$= \boxed{\frac{1}{32}N^5 + \frac{5}{8}N^4 + 5N^3 + 20N^2 + 40N + 32}$$