

BE-PRECALC TUESDAY 10-13-09

SIMPLIFY

EXPONENT RULE TO USE

① $x^4 y^8 (x^2 y^2)$

MR $\Rightarrow a^m a^n = a^{m+n}$

② $\frac{x^4 y^8}{x^2 y^2}$

DR $\Rightarrow \frac{a^m}{a^n} = a^{m-n}$

③ $\frac{x^4 y^8}{x^4 y^8}$

ZER $\Rightarrow a^0 = 1$ EXCEPT $0^0 = 0$

④ $\frac{x^2 y^2}{x^4 y^4}$

NER $\Rightarrow a^{-n} = \frac{1}{a^n}$

⑤ 6^{-2}

⑥ $\frac{1}{6^{-2}}$

⑦ $(x^4 y^8)^2$

PP $\Rightarrow (a^n)^m = a^{n \cdot m}$

⑧ $\left(\frac{x^4 y^8}{x^2 y^2}\right)^2$

GP $\Rightarrow (ab)^n = a^n b^n$

or $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$

SEE/MEMORIZE EXPONENT RULES HANDOUT
*VERY USEFUL FOR ACT!

Summary of Exponent Rules

Multiplication
Rule

$$a^m \cdot a^n = a^{m+n}$$

EX) $(x^4 y^3)(x^5 y) = x^9 y^4$

EX) $8^3 \cdot 8^7 = 8^{10}$

Division
Rule

$m > n$

$$\frac{a^m}{a^n} = a^{m-n}$$

EX) $\frac{x^8}{x^3} = x^5$

EX) $\frac{5^{12}}{5^4} = 5^8$

Zero Exponent
Rule

Division Rule
where $m = n$

$$a^0 = 1$$

EXCEPT FOR
 $0^0 = 0$

EX) $(4x^3 y)^0 = 1$

EX) $5^0 = 1$

Negative Exponent
Rule

Division Rule
where $m < n$

$$a^{-n} = \frac{1}{a^n}$$

EX) $5^{-2} = \frac{1}{5^2} = \frac{1}{25}$

EX) $4x^{-3} = 4 \cdot \frac{1}{x^3} = \frac{4}{x^3}$

💡 Never LEAVE A
NEGATIVE EXPONENT

Power To A Power
Rule

$$(a^m)^n = a^{m \cdot n}$$

EX) $(5^2)^5 = 5^{10}$

EX) $[(4^3)^2]^6 = [4^6]^6 = 4^{36}$

Group To A Power
Rule

$$(ab)^n = a^n b^n$$

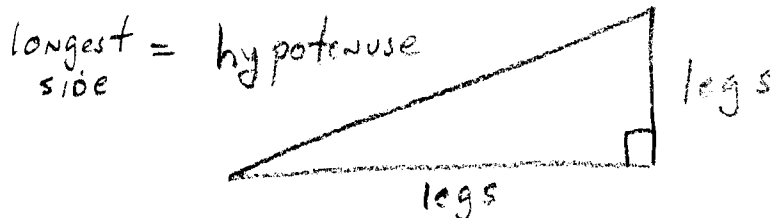
OR
 $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$

EX) $(4x)^2 = 4^2 x^2 = 16x^2$

EX) $\left(\frac{2x}{y}\right)^3 = \frac{2^3 x^3}{y^3} = \frac{8x^3}{y^3}$

Right Triangle Vocabulary AND Conventions & Properties

" $\square$ " 90° symbol (EX) 

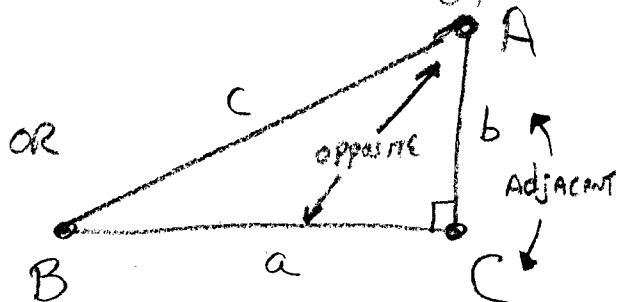
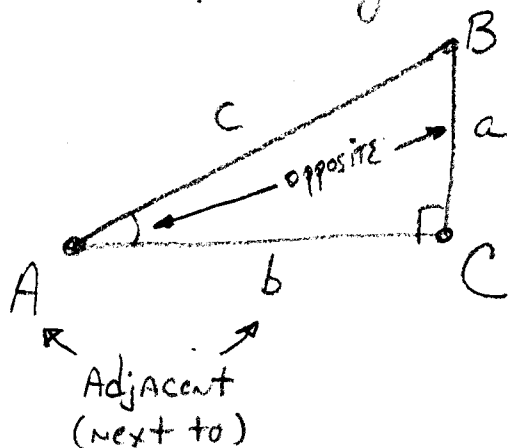


Every right triangle has ONE 90° angle
(90°)
and two acute ($< 90^\circ$) angles. The two
acute angles always add to 90° and
together with the 90° angle = 180°

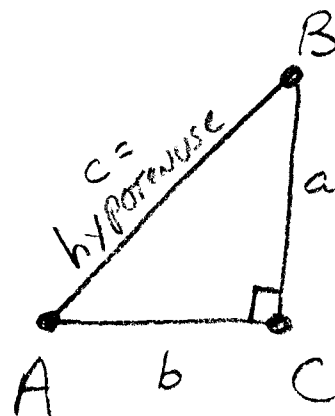
A, B, C = vertices or the angles (degrees)

a, b, c = sides (length)

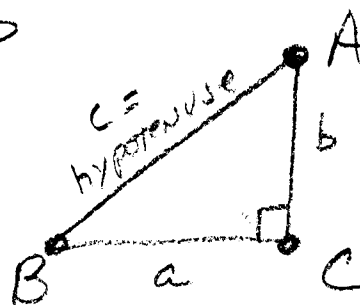
C = the 90° angle by convention $\therefore$ c = hypotenuse



- Adjacent and opposite are never used to describe the hypotenuse. The hypotenuse is called the...
hypotenuse

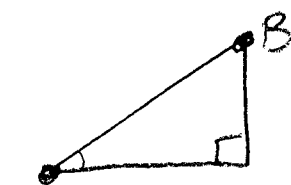


- $\angle A$ is always opposite side a (and adjacent to side b) (Angle A)
- $\angle B$ is always opposite side b (and adjacent to side a)



In any right triangle, once you know ONE acute angle - you know all 3 angles.

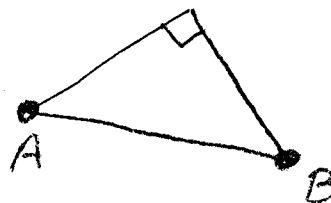
(EX) Name the missing $\angle$ value



$$\begin{aligned} A &= 40^\circ \\ B &= ? \\ C &= ? \end{aligned}$$

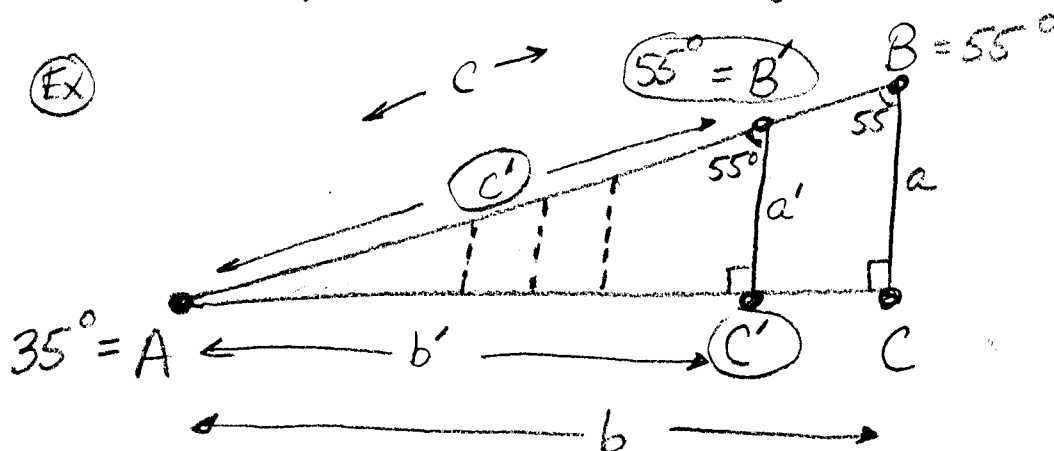


$$\begin{aligned} A &= 10^\circ \\ B &= ? \\ C &= ? \end{aligned}$$



$$\begin{aligned} A &= 45^\circ \\ B &= ? \\ C &= ? \end{aligned}$$

BECAUSE KNOWING the VALUE of 1 ACUTE angle "fixes" the VALUE of THE OTHER two angles, for ANY given ACUTE angle, say 35° , the RATIO of side lengths of ALL $35^\circ, 55^\circ, 90^\circ$ triangles ARE the SAME:



- INFINITE NUMBER OF $35^\circ-55^\circ-90^\circ$ triangles but the ratio of sides is always the same number

$$\text{For } A = 35^\circ, \quad \frac{a}{c} = \frac{a'}{c'} = \frac{\text{Any } a}{\text{Any } c} \approx .5736$$

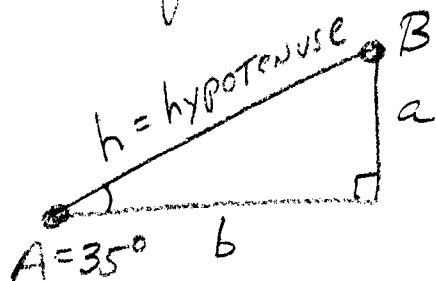
$$\frac{b}{c} = \frac{b'}{c'} = \frac{\text{Any } b}{\text{Any } c} \approx .8192$$

$$\frac{a}{b} = \frac{a'}{b'} = \frac{\text{Any } a}{\text{Any } b} \approx .7002$$

$\nearrow$
 $\frac{\text{RISE}}{\text{RUN}}$ of $A = \text{SLOPE}$, slope of $45^\circ = 1$
 slope of $35^\circ = < 1$ but close

Since, for any PARTICULAR ACUTE angle in a right triangle the RATIO OF THE lengths of the sides are always the same, we NAME AND define them.

For THIS example:



$$\text{SINE} = \sin A = \sin 35^\circ = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{o}{h} \approx .5736 \quad (\text{SOH})$$

$$\text{COSINE} = \cos A = \cos 35^\circ = \frac{\text{Adjacent}}{\text{hypotenuse}} = \frac{a}{h} \approx .8192 \quad (\text{CAH})$$

$$\text{tangent} = \tan A = \tan 35^\circ = \frac{\text{opposite}}{\text{adjacent}} = \frac{o}{a} \approx .7002 \quad (\text{TOA})$$

(Slope)

For any right triangle, where θ is an ACUTE $\angle$ theta = greek letter

$$\sin \theta = \frac{o}{h} \quad \cos \theta = \frac{a}{h} \quad \tan \theta = \frac{o}{a}$$

SOH	CAH	TOA
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FIND: $\sin, \cos, \tan 35^\circ$ from: table (handout)
 calculator
 (bring ACT calculator)

SOH CAH TOA

 $\sin = o/h$ $\cos = a/h$
 $\tan = o/a = \text{rise/run}$
 $\tan(0) = 0, \tan(90) = \text{undefined}, \tan(45) = 1$

Table : Trigonometric Functions

Use for angles
between 0 and
45 degrees.

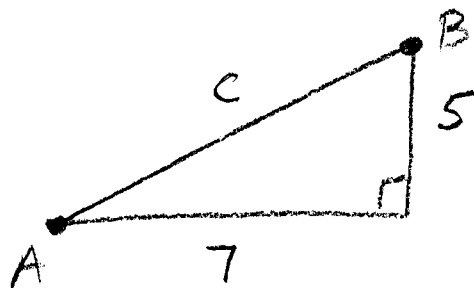
Degrees	Radians	Sin	Cos	Tan	Cot	
0	0.0000	0.0000	1.0000	0.0000		1.5708
1	0.0175	0.0175	0.9998	0.0175	57.290	1.5533
2	0.0349	0.0349	0.9994	0.0349	28.636	1.5359
3	0.0524	0.0523	0.9986	0.0524	19.081	1.5184
4	0.0698	0.0698	0.9976	0.0699	14.301	1.5010
5	0.0873	0.0872	0.9962	0.0875	11.430	1.4835
6	0.1047	0.1045	0.9945	0.1051	9.5144	1.4661
7	0.1222	0.1219	0.9925	0.1228	8.1443	1.4486
8	0.1396	0.1392	0.9903	0.1405	7.1154	1.4312
9	0.1571	0.1564	0.9877	0.1584	6.3138	1.4137
10	0.1745	0.1736	0.9848	0.1763	5.6713	1.3963
11	0.1920	0.1908	0.9816	0.1944	5.1446	1.3788
12	0.2094	0.2079	0.9781	0.2126	4.7046	1.3614
13	0.2269	0.2250	0.9744	0.2309	4.3315	1.3439
14	0.2443	0.2419	0.9703	0.2493	4.0108	1.3265
15	0.2618	0.2588	0.9659	0.2679	3.7321	1.3090
16	0.2793	0.2756	0.9613	0.2867	3.4874	1.2915
17	0.2967	0.2924	0.9563	0.3057	3.2709	1.2741
18	0.3142	0.3090	0.9511	0.3249	3.0777	1.2566
19	0.3316	0.3256	0.9455	0.3443	2.9042	1.2392
20	0.3491	0.3420	0.9397	0.3640	2.7475	1.2217
21	0.3665	0.3584	0.9336	0.3839	2.6051	1.2043
22	0.3840	0.3746	0.9272	0.4040	2.4751	1.1868
23	0.4014	0.3907	0.9205	0.4245	2.3559	1.1694
24	0.4189	0.4067	0.9135	0.4452	2.2460	1.1519
25	0.4363	0.4226	0.9063	0.4663	2.1445	1.1345
26	0.4538	0.4384	0.8988	0.4877	2.0503	1.1170
27	0.4712	0.4540	0.8910	0.5095	1.9626	1.0996
28	0.4887	0.4695	0.8829	0.5317	1.8807	1.0821
29	0.5061	0.4848	0.8746	0.5543	1.8040	1.0647
30	0.5236	0.5000	0.8660	0.5774	1.7321	1.0472
31	0.5411	0.5150	0.8572	0.6009	1.6643	1.0297
32	0.5585	0.5299	0.8480	0.6249	1.6003	1.0123
33	0.5760	0.5446	0.8387	0.6494	1.5399	0.9948
34	0.5934	0.5592	0.8290	0.6745	1.4826	0.9774
35	0.6109	0.5736	0.8192	0.7002	1.4281	0.9599
36	0.6283	0.5878	0.8090	0.7265	1.3764	0.9425
37	0.6458	0.6018	0.7986	0.7536	1.3270	0.9250
38	0.6632	0.6157	0.7880	0.7813	1.2799	0.9076
39	0.6807	0.6293	0.7771	0.8098	1.2349	0.8901
40	0.6981	0.6428	0.7660	0.8391	1.1918	0.8727
41	0.7156	0.6561	0.7547	0.8693	1.1504	0.8552
42	0.7330	0.6691	0.7431	0.9004	1.1106	0.8378
43	0.7505	0.6820	0.7314	0.9325	1.0724	0.8203
44	0.7679	0.6947	0.7193	0.9657	1.0355	0.8029
45	0.7854	0.7071	0.7071	1.0000	1.0000	0.7854
		Cos	Sin	Cot	Tan	Radians
						Degrees

Use for angles
between 45 and
90 degrees.

SOHCAHTOA

ⓔ Find $\sin$, $\cos$, $\tan$ for $\angle A$ and $\angle B$

(Find EXACT value = simplified fraction, then compare with value from table & calculator)



$$c^2 = a^2 + b^2 \quad \therefore c^2 = 49 + 25$$

$$c = \sqrt{74} \sim 8.6023$$

$$\sin A = \frac{o}{h} = \frac{\text{EXACT}}{\frac{5}{\sqrt{74}}} = \frac{5}{\sqrt{74}} \cdot \frac{\sqrt{74}}{\sqrt{74}} = \frac{\text{EXACT}}{\frac{5\sqrt{74}}{74}}$$

"RATIONALIZED"
NO $\sqrt{}$ in bottom

$$\approx \frac{5}{8.6023} \approx \frac{\text{APPROXIMATE}}{.5812}$$

$$\cos A = \frac{a}{h} = \frac{7}{\sqrt{74}} = \frac{\text{EXACT}}{\frac{7\sqrt{74}}{74}} \approx \frac{7}{8.6023} = \frac{\text{APPROXIMATE}}{.8137}$$

$$\tan A = \frac{o}{a} = \frac{\text{EXACT}}{\frac{5}{7}} \approx \frac{\text{APPROXIMATE}}{.7142}$$

$$\sin B = \frac{7}{\sqrt{74}} \quad \cos B = \frac{5}{\sqrt{74}}$$

See ABOVE
FOR EXACT AND APPROXIMATE

* NOW
CAREFUL

$$\tan B = \text{slope } B = \frac{o}{a} = \frac{\text{EXACT}}{\frac{7}{5}} = \frac{\text{EXACT}}{1.4} \quad \text{WHY IS ONE } \tan > 1 \text{ AND ONE IS } < 1 ?$$

7.
If $\sin A \approx .5812$ CAN you find $\angle A$?

Using table $\Rightarrow$ find a SIN VALUE OF
.5812 (closest to it)
and read angle $\approx \underline{\underline{36^\circ}}$

The process of going backward
from the value of the sin to
the angle is called finding
the inverse of the sin $\Rightarrow \sin^{-1} A$
OR sometimes it is called the

$$\text{ARCSIN } A \quad \therefore \sin^{-1}(.5812) = \text{ARCSIN}(.5812) = 36^\circ$$

$$\therefore \angle B = 90 - 36 = 54^\circ$$

• Homework $\Rightarrow$ Pg 288 #10-13, 20-22.