

# 4-5 Study Guide and Intervention

## Graphing Linear Equations

**Identify Linear Equations** A linear equation is an equation that can be written in the form  $Ax + By = C$ . This is called the **standard form** of a linear equation.

**Standard Form of a Linear Equation**

$Ax + By = C$ , where  $A \geq 0$ ,  $A$  and  $B$  are not both zero, and  $A$ ,  $B$ , and  $C$  are integers whose GCF is 1.

### Example 1

Determine whether  $y = 6 - 3x$  is a linear equation. If so, write the equation in standard form.

First rewrite the equation so both variables are on the same side of the equation.

$$\begin{array}{ll} y = 6 - 3x & \text{Original equation} \\ y + 3x = 6 - 3x + 3x & \text{Add } 3x \text{ to each side.} \\ 3x + y = 6 & \text{Simplify.} \end{array}$$

The equation is now in standard form, with  $A = 3$ ,  $B = 1$  and  $C = 6$ . This is a linear equation.

### Example 2

Determine whether  $3xy + y = 4 + 2x$  is a linear equation. If so, write the equation in standard form.

Since the term  $3xy$  has two variables, the equation cannot be written in the form  $Ax + By = C$ . Therefore, this is not a linear equation.

### Exercises

*\*THE "NOT LINEARS" CAN BE SHOWN ON THIS PAGE.  
ALL OTHERS MUST BE ON LOOSE LEAF.*

\* Determine whether each equation is a linear equation. If so, write the equation in standard form.

1.  $2x = 4y$

2.  $6 + y = 8$

3.  $4x - 2y = -1$

4.  $3xy + 8 = 4y$

5.  $3x - 4 = 12$

6.  $y = x^2 + 7$

7.  $y - 4x = 9$

8.  $x + 8 = 0$

9.  $-2x + 3 = 4y$

10.  $2 + \frac{1}{2}x = y$

11.  $\frac{1}{4}y = 12 - 4x$

12.  $3xy - y = 8$

13.  $6x + 4y - 3 = 0$

14.  $yx - 2 = 8$

15.  $6a - 2b = 8 + b$

16.  $\frac{1}{4}x - 12y = 1$

17.  $3 + x + x^2 = 0$

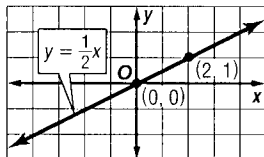
18.  $x^2 = 2xy$

**5-2 Study Guide and Intervention****Slope and Direct Variation**

**Direct Variation** A direct variation is described by an equation of the form  $y = kx$ , where  $k \neq 0$ . We say that  $y$  *varies directly as*  $x$ . In the equation  $y = kx$ ,  $k$  is the **constant of variation**.

**Example 1**

Name the constant of variation for the equation. Then find the slope of the line that passes through the pair of points.



For  $y = \frac{1}{2}x$ , the constant of variation is  $\frac{1}{2}$ .

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Slope formula}$$

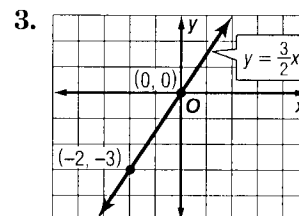
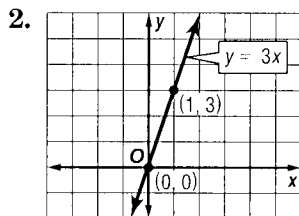
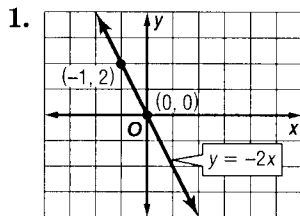
$$= \frac{1 - 0}{2 - 0} \quad (x_1, y_1) = (0, 0), (x_2, y_2) = (2, 1)$$

$$= \frac{1}{2} \quad \text{Simplify.}$$

The slope is  $\frac{1}{2}$ .

**Exercises**

Name the constant of variation for each equation. Then determine the slope of the line that passes through each pair of points.



**ANSWER BOTH PARTS!**

\* **a.** Write a direct variation equation that relates  $x$  to  $y$ . Assume that  $y$  varies directly as  $x$ . Then solve.

4. If  $y = 4$  when  $x = 2$ , find  $y$  when  $x = 16$ .

5. If  $y = 9$  when  $x = -3$ , find  $x$  when  $y = 6$ .

6. If  $y = -4.8$  when  $x = -1.6$ , find  $x$  when  $y = -24$ .

7. If  $y = \frac{1}{4}$  when  $x = \frac{1}{8}$ , find  $x$  when  $y = \frac{3}{16}$ .

**Example 2**

Suppose  $y$  varies directly as  $x$ , and  $y = 30$  when  $x = 5$ .

**a.** Write a direct variation equation that relates  $x$  and  $y$ .

Find the value of  $k$ .

$$y = kx \quad \text{Direct variation equation}$$

$$30 = k(5) \quad \text{Replace } y \text{ with 30 and } x \text{ with 5.}$$

$$6 = k \quad \text{Divide each side by 5.}$$

Therefore, the equation is  $y = 6x$ .

**b.** Use the direct variation equation to find  $x$  when  $y = 18$ .

$$y = 6x \quad \text{Direct variation equation}$$

$$18 = 6x \quad \text{Replace } y \text{ with 18.}$$

$$3 = x \quad \text{Divide each side by 6.}$$

Therefore,  $x = 3$  when  $y = 18$ .