

BE - Geometry I - Monday

4-23-12

① Define a function.

② Define the domain and range of a function.

③ If $y = f(x) = 3x^2$

$$y = g(x) = 2x - 1$$

Ⓐ $f(-3) = ?$

Ⓑ $g(0) = ?$

Ⓒ $f[g(x)] = (f \circ g)(x) = ?$

$$f(g(x)) \Rightarrow f(x) = 3x^2$$

$$\nearrow f(2x-1) = 3(2x-1)^2$$

$$= 3[4x^2 - 4x + 1]$$

$$= \boxed{12x^2 - 12x + 3}$$

The
Composition
of f and g

A function is a set of ordered pairs where each x is paired with one unique y .

Ex

X	Y
2	6
4	-1
0	6
3	5
9	-4
π	$\sqrt{3}$

Graphs of functions pass the
VLT \Rightarrow vertical line test.

Can you name some functions we have covered so far?

OK, for these functions, give their name, domain, and range:

$$y = f(x) = ax + b \quad \text{LINEAR function}$$

$$d = \mathbb{R}, r = \mathbb{R}$$

$$y = f(x) = ax^2 + bx + c \quad \text{quadratic function}$$

$$d = \mathbb{R}, r = \mathbb{P}$$

$$y = f(x) = |x| \quad \text{Absolute value function}$$

$$d = \mathbb{R}, r = y \geq 0$$

$$y = f(x) = \sin(x) \quad \text{SINE function}$$

$$d = \mathbb{R}, r = -1 \leq y \leq 1$$

$$y = f(x) = \text{ARCSIN}(x) \quad \text{ARCSIN function}$$

$$d = -1 \leq x \leq 1 \quad r = \mathbb{R}$$

or INVERSE SINE function

$$y = f(x) = b^x \quad \text{EXPONENTIAL function}$$

$$d = \mathbb{P} \quad r = y > 0$$

$$y = f(x) = \log_b x \quad \text{LOGARITHMIC function}$$

or INVERSE EXPONENTIAL funct.

$$d = x > 0 \quad y = \mathbb{R}$$

So WHAT IS AN inverse function?

Inverse Function Two functions ARE inverse if, for every ordered pair (a, b) in one function, the other function contains (b, a)

Symbol
 $f^{-1}(x)$

In other words, the X and Y values ARE swapped for every (x, y)

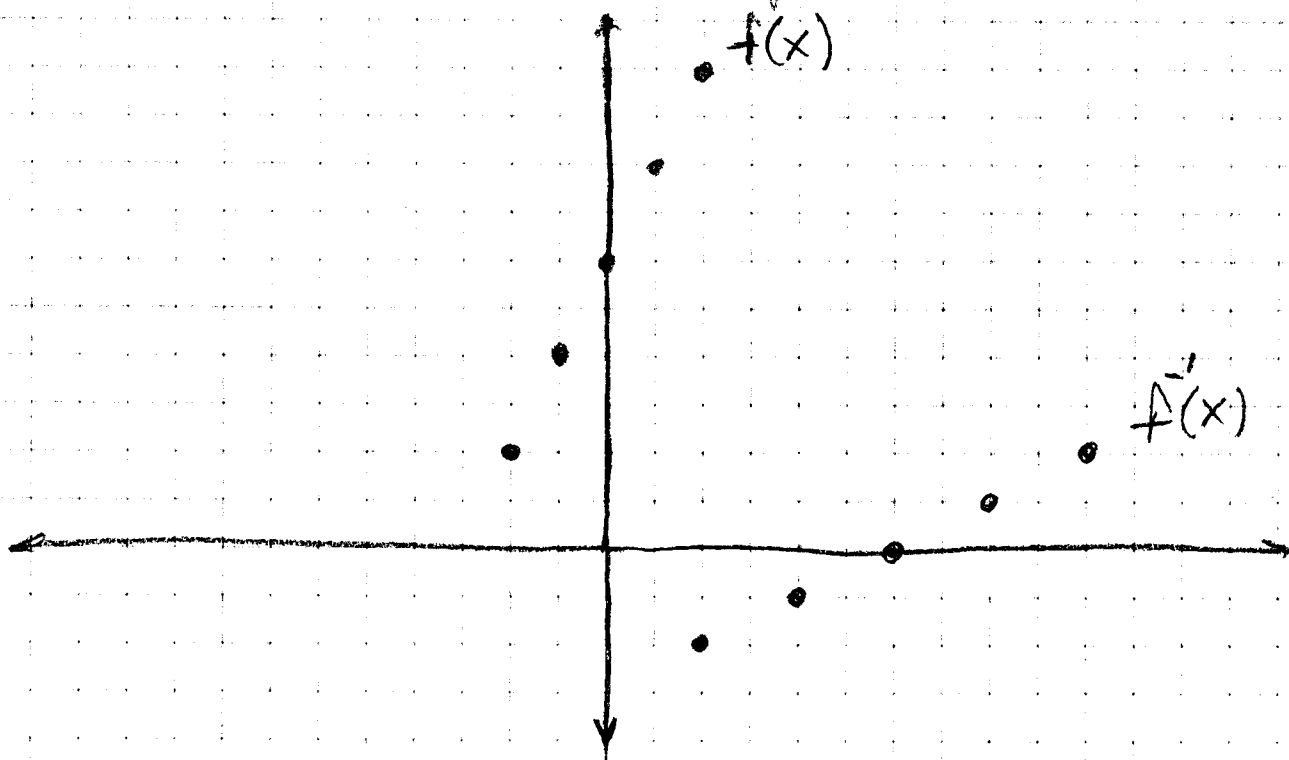
Ex) $f(x)$

x	y
-2	2
-1	4
0	6
1	8
2	10

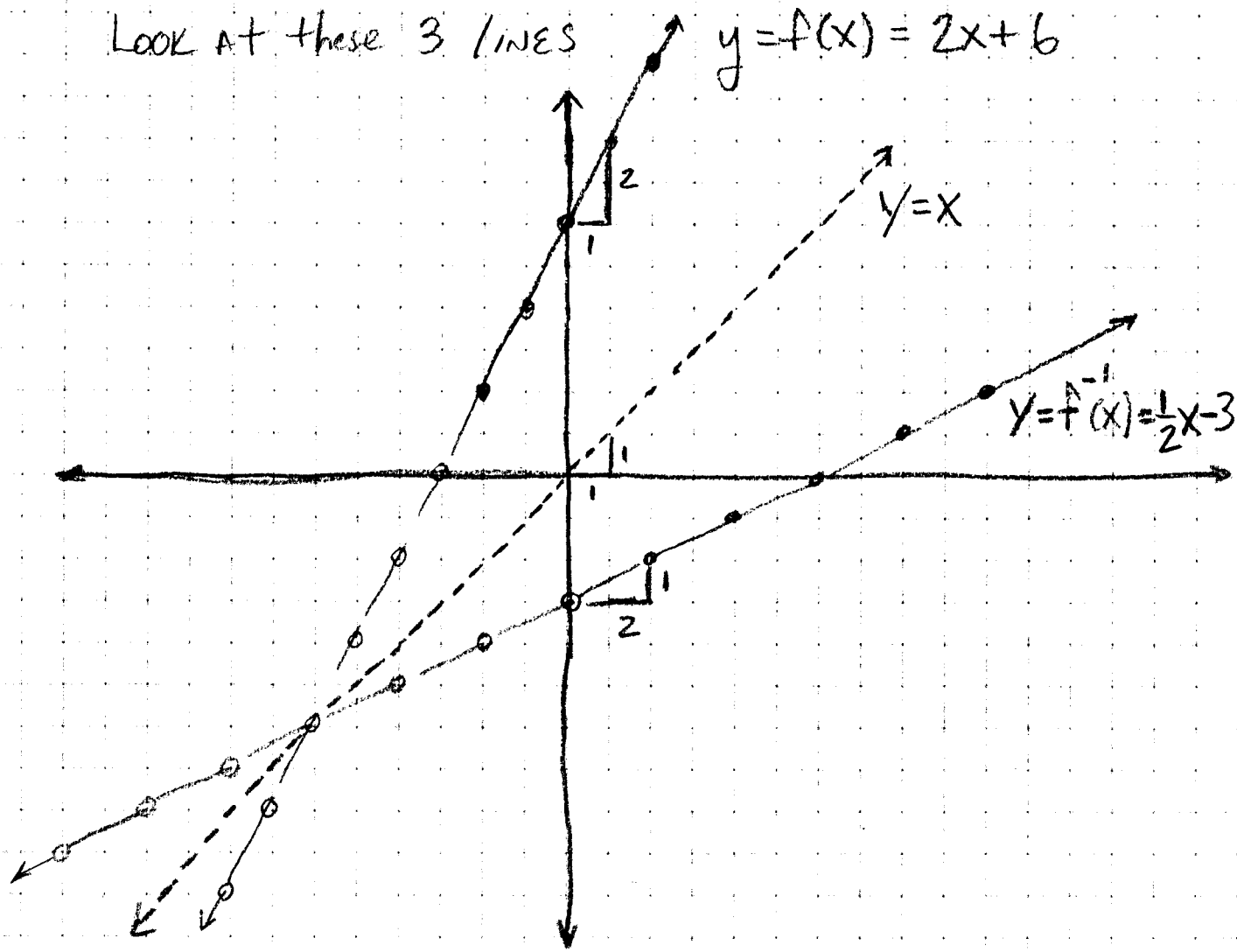
$f^{-1}(x)$

x	y
2	-2
4	-1
6	0
8	1
10	2

IS THERE A RELATIONSHIP?



LOOK AT THESE 3 LINES



INVERSE FUNCTIONS ARE ALWAYS
symmetrical about the line $y=x$

NOT ALL FUNCTIONS HAVE INVERSE
FUNCTIONS BUT ... HERE IS HOW TO
FIND THEM:

⊙ $y = f(x) = 2x + 6$

↓ swap x and y and solve
for y

$$x = 2y + 6$$

$$\frac{x-6}{2} = \frac{2y}{2}$$

$$\frac{1}{2}x - 3 = y = f^{-1}(x)$$

Find the inverse AND graph both functions - show they are symmetrical to a dashed line $y=x$

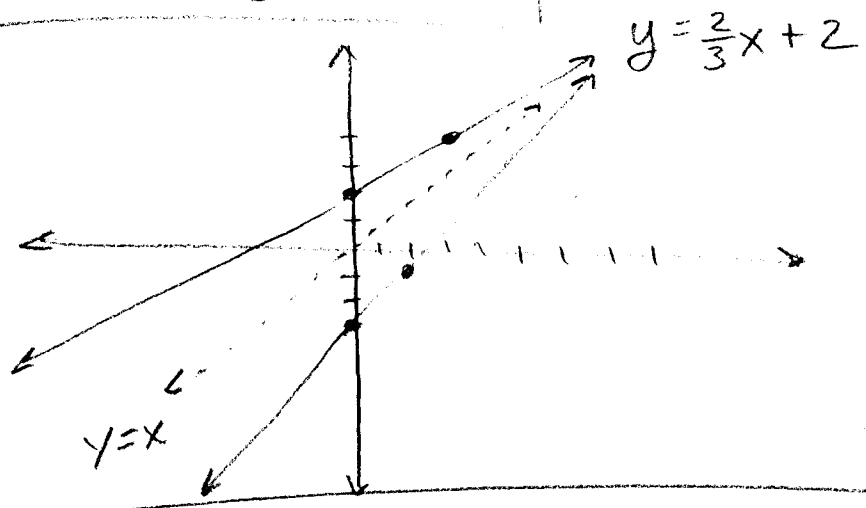
$$y = f(x) = \frac{2}{3}x + 2$$

$$f^{-1}(x) \Rightarrow x = \frac{2}{3}y + 2$$

$$x - 2 = \frac{2}{3}y$$

$$\frac{3}{2}(x - 2) = y$$

$$y = f^{-1}(x) = \frac{3}{2}x - 3$$



Homework: Find $f^{-1}(x)$ and graph both with $y=x$

- ① $y = 2x - 4$
- ② $y = \frac{1}{2}x + 3$
- ③ $y = 4x - 1$
- ④ $y = -\frac{3}{4}x + 6$